

# Transverse Momentum Spectra and Elliptic flow in ideal hydrodynamics and Geometric Scaling

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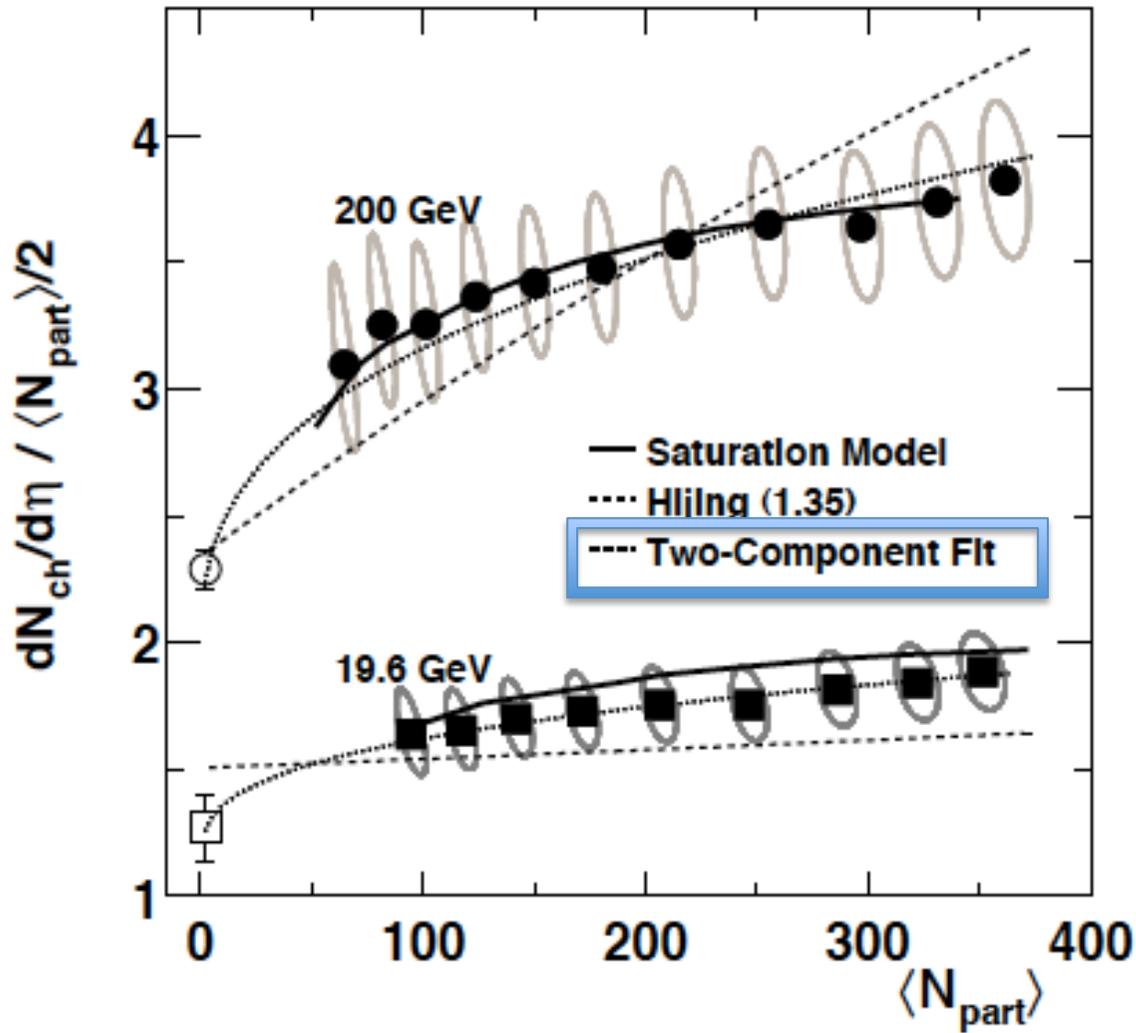
In collaboration with Dr. A.K.Chaudhuri

# Plan of Talk

- Introduction
- Initial conditions
- hydrodynamics
- Result
- Summary and conclusion

# Introduction

PHOBOS: Charged particle multiplicity



$$\frac{dN}{d\eta} = n_{pp} \left[ (1-x) \frac{N_{part}}{2} + x N_{coll} \right] \dots\dots\dots(1)$$

$x \rightarrow$  Fraction of hard scattering

Soft process  $\sim N_{part}$   
 Hard process  $\sim N_{coll}$

D. Kharzeev and M.Nardi  
 Phys. Lett. B, 507,121

Dependence of x on beam energy

Beam Energy (GeV)	X
*19.6	$0.13 \pm 0.01 \pm 0.05$
56	$0.05 \pm 0.03$
130	$0.09 \pm 0.03$
*200	$0.13 \pm 0.01 \pm 0.05$

\* PHOBOS

## Application in hydrodynamic model

Geometric scaling of Au+Au collisions as in equation (1), has been widely Used in hydrodynamic model calculation

❖ P. F. Kolb, U. W. Heinz, P. Huovinen, K. J. Eskola and K. Tuominen, Nucl. Phys. A 696, 197 (2001).

❖ T. Hirano and Y. Nara, Phys. Rev. C 79, 064904 (2009)

## Glauber initial condition and ideal hydrodynamics

- Hydrodynamics model require initial energy density configuration.

$$\varepsilon(b,x,y) = \varepsilon_0 \left[ (1-x)N_{part}(b,x,y) + xN_{coll}(b,x,y) \right] \dots\dots\dots(2)$$

$\varepsilon_0$  is the central energy density in  $\mathbf{b}=0$  collision

➤ **current status :**

- hard scattering fraction  $x=0.25$  explains a variety of experimental data, e.g. identified particle's multiplicity ,mean transverse momentum, elliptic flow etc.

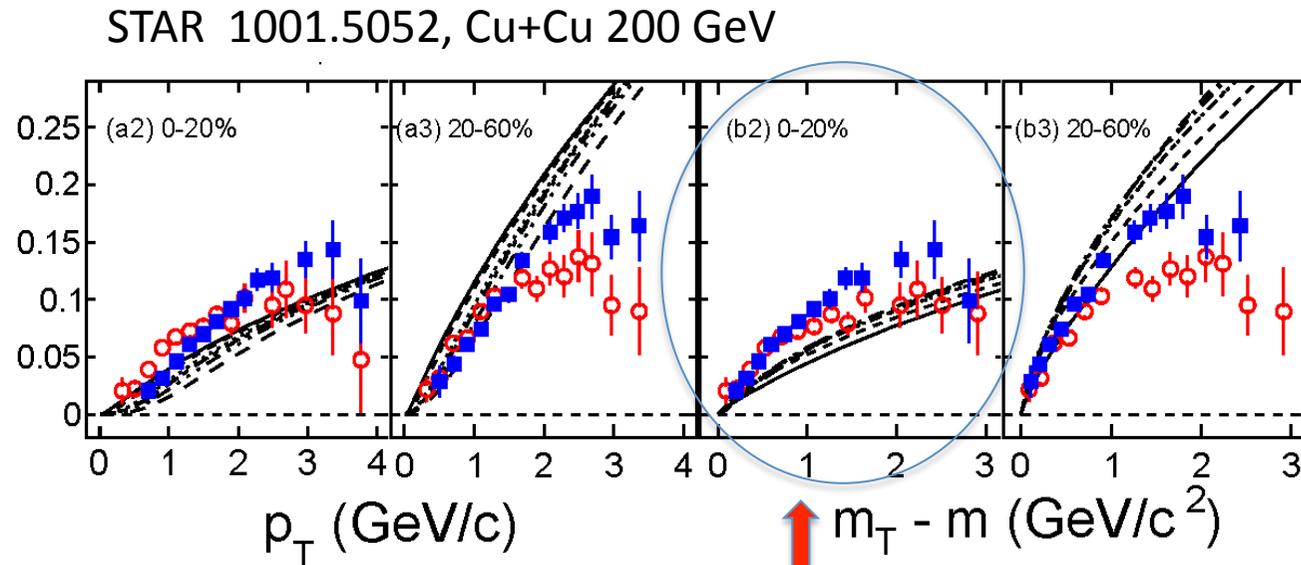
P. F. Kolb and U. Heinz, in Quark-Gluon Plasma 3  
edited by R. C. Hwa and X.-N. Wang (World Scientific,Singapore, 2004), p. 634

- With  $x=0.13$ , also gives reasonable description to the experimental data.

T. Hirano and Y. Nara, Phys. Rev. C 79, 064904 (2009)

**This work extends this investigation**

# Ideal hydro and elliptic flow



- ◆ Glauber initial condition with  $x=0.13$  and  $x=0.25$  fails to explain central collision.
- ◆ Elliptic flow is a key observable to established the existence of partonic medium and address the issue of thermalization in Au+Au collision
- ◆ **Important to understand why Glauber model initial condition underestimate Elliptic flow in very central collision**
- ◆ Inclusion of dissipative effect will not improve the situation as it will only reduce  $v_2$

# Hydrodynamic simulation with Glauber model initialization

## Current Study :

$$\partial_{\mu} T^{\mu\nu} = 0 \quad \dots\dots\dots(3)$$

- We have simulated 200 GeV Au+Au collisions
- with Glauber model initial condition at two extreme limit of the hard scattering fraction

x=0 ~ soft process

x=1 ~ hard process

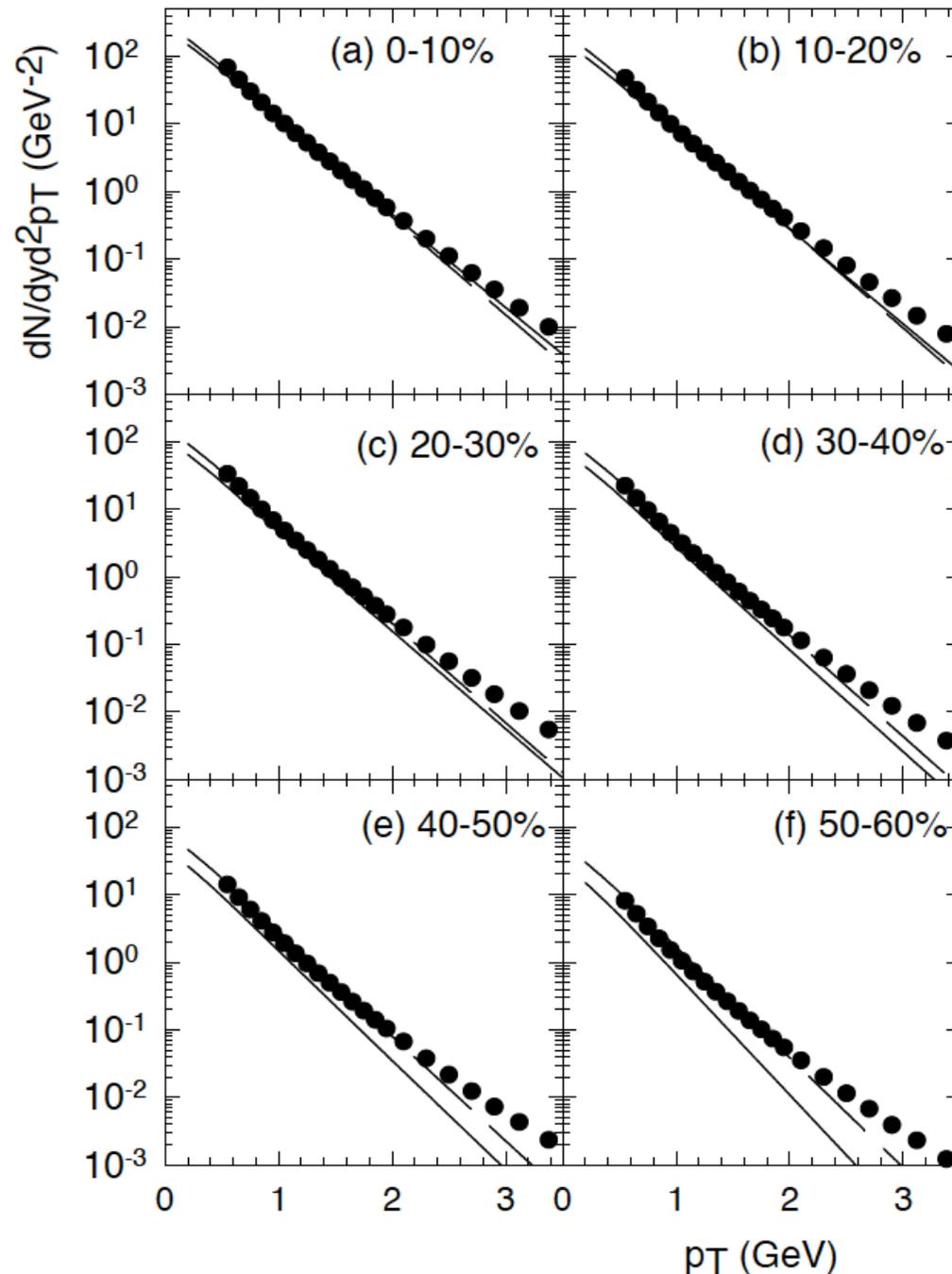
$$\varepsilon(b,x,y) = \varepsilon_0 \left[ (1-x)N_{part}(b,x,y) + xN_{coll}(b,x,y) \right]$$

- We assume that in Au+Au collisions, a 'baryonless', 'ideal' QGP fluid is produced.

## Assumptions and initial conditions

- **Coordinate system** :  $\tau = \sqrt{t^2 - z^2}$  ,  $x, y$ ,  $\eta = \frac{1}{2} \ln \frac{t+z}{t-z}$
- **Longitudinal boost invariant** :  $\eta$  symmetry
- **EOS** : lattice+HRG EOS ,  $T_{co}=196$  MeV  
lattice-(2+1)  
Hadron gas (mass  $\leq 2.5$  GeV)  
*M. Cheng et al., Phys. Rev. D 77, 014511*
- **Initial time** :  $\tau_i = 0.6$  fm
- **Initial fluid velocity** :  $v_x(x,y) = v_y(x,y) = 0$
- **Freeze-out temperature** :  $T_F=150$  MeV.
- **Initial central energy density** :  
 $\epsilon_0 = 36.1$  GeV/fm<sup>3</sup> ,  $x=0$   
 $\epsilon_0 = 48$  GeV/fm<sup>3</sup> ,  $x=1$

# Charged Hadron $p_T$ spectra, 200 GeV, Au+Au (PHENIX)



✓ Dashed lines

$$x=0$$

$$\varepsilon_0 = 36.1 \text{ GeV} / \text{fm}^3$$

✓ Solid line

$$x=1$$

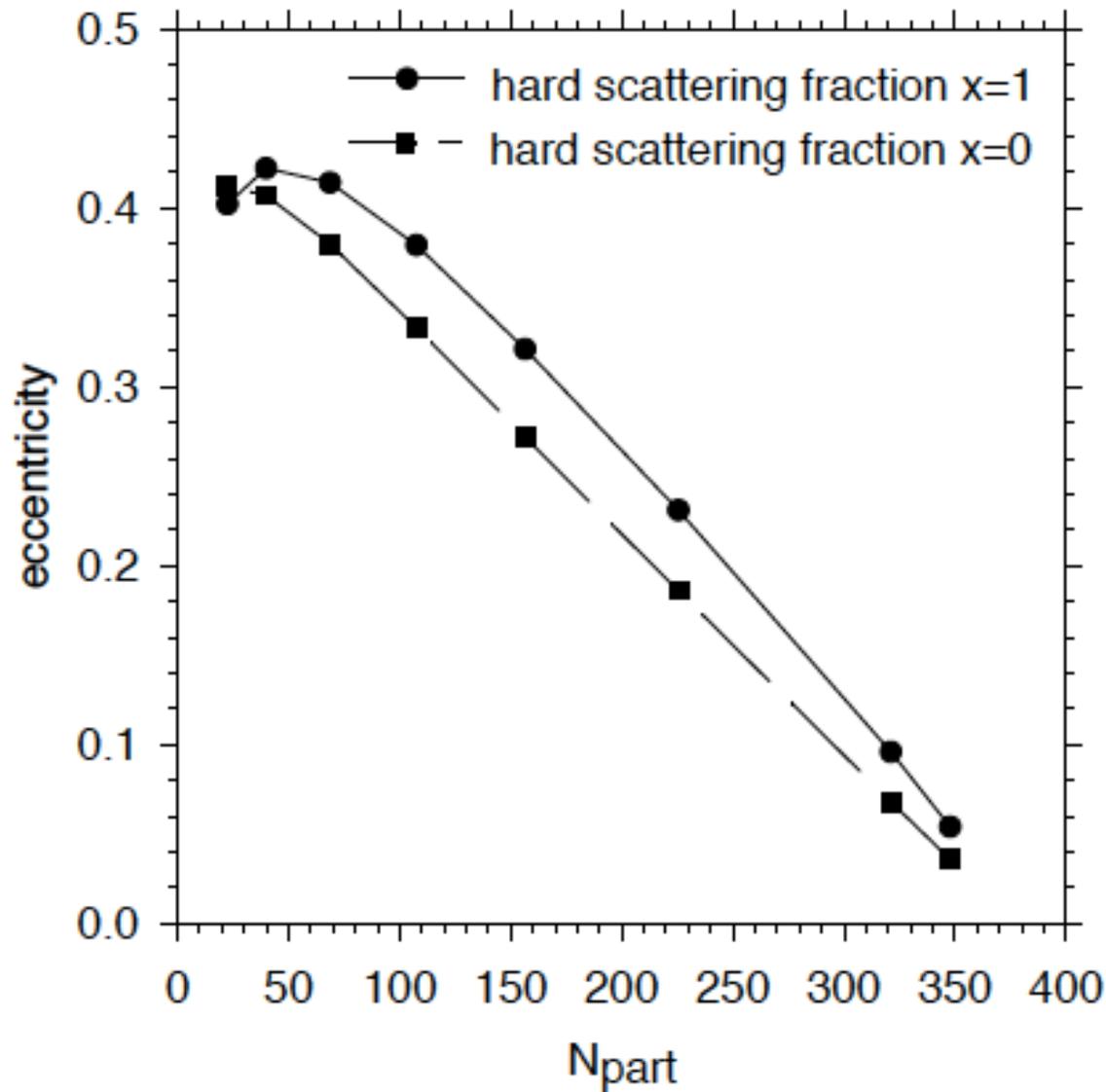
$$\varepsilon_0 = 48 \text{ GeV} / \text{fm}^3$$

➤ 0-10% reasonable fit in both scenario

➤ Different behavior in peripheral collision

\*S. S. Adler et al. [PHENIX Collaboration], Phys. Rev. C 69, 034910 (2004)

# Elliptic flow and Initial Spatial Eccentricity



Ideal hydrodynamics:

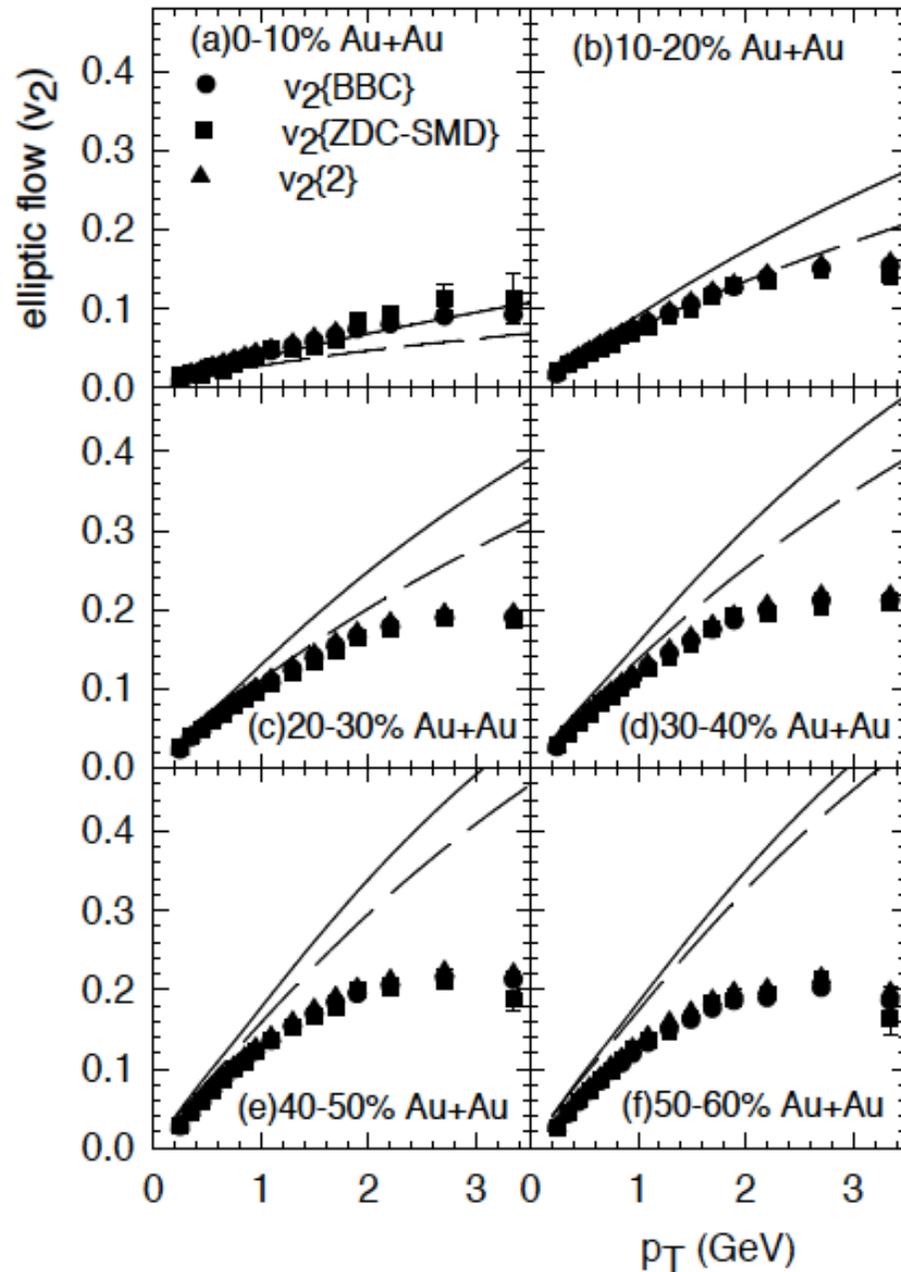
$$v_2 \propto \mathcal{E}_x$$

$$\mathcal{E}_x = \frac{\langle y^2 - x^2 \rangle}{\langle y^2 + x^2 \rangle}$$

$\langle \dots \rangle$  Denotes energy density weighted averaging

Initial eccentricity are different for two scenario

## Charged particle $v_2$ , 200 GeV, Au+Au (PHENIX)



❖ The solid line  $\rightarrow x = 1$

❖ The dashed line  $\rightarrow x = 0$

❖ Other conditions same as for charged hadron  $p_T$  spectra

$x = 1$  -- data is over predicted for higher centrality .

10-20% ,  $P_T=1.5$  GeV  $\sim 20\%$  higher  
 50-60% at  $P_T=1.5$  GeV  $\sim 60\%$  higher

$x = 0$  --data under predicted  
 0-10% --  $P_T=1.5$  GeV  $\sim 35\%$

\*S. Afanasiev et al. [PHENIX Collaboration],  
 Phys. Rev.C 80, 024909 (2009).

- Present analysis indicate that in 0-10% Au+Au collisions, simultaneous description of the  $p_T$  spectra and elliptic flow require hard scattering fraction  $x = 1$  in the Glauber model initial condition.
- However less central collision,  $x = 0$  ,better describe  $v_2$  and  $p_T$
- Geometric scaling of Au+Au collisions changes with collision centrality. Arguably, transition from binary collision number scaling to participant scaling can not be as sharp as conjectured here.

**and**

More detailed analysis is required to find the width and exact location of the transition.

## Few comments

- In the present analysis we have not included eccentricity fluctuation.
- Hirano and Nara\* have studied the effect of eccentricity fluctuation on elliptic flow. They found Glauber model initialization ( 13% hard scattering fraction), even with eccentricity fluctuation, under predict experimental (integrated) elliptic flow.

\*T. Hirano and Y. Nara, Phys. Rev. C 79, 064904 (2009).

- We have estimated the effect of eccentricity fluctuations on differential elliptic flow . With participant scaling(  $x = 0$  ),in 0-10% collision, in the  $p_T$  range 1-2 GeV, elliptic flow increases only by  $\approx 10\%$ . Experimental flow are still under predicted.
- Other models of initials condition like CGC, Quark participant .

## Summary and conclusion

- ❖ Two extreme scenarios with Glauber model initialization in ideal hydrodynamic are considered

$$\varepsilon(b, X, Y) = \varepsilon_0 \left[ (1 - x) N_{part}(b, X, Y) + x N_{coll}(b, X, Y) \right]$$

$x = 1$   Hard processes

$x = 0$   Soft processes

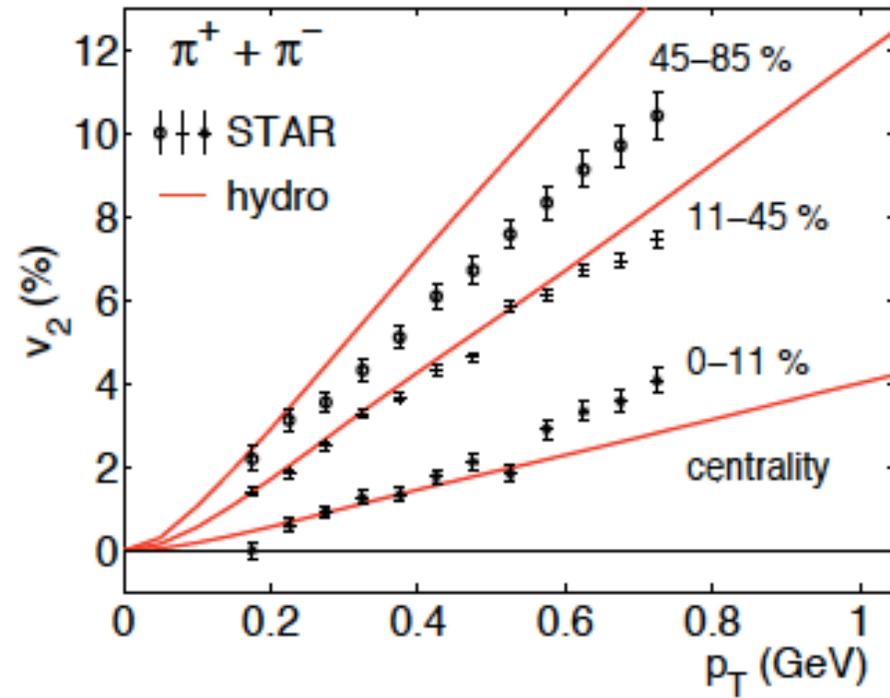
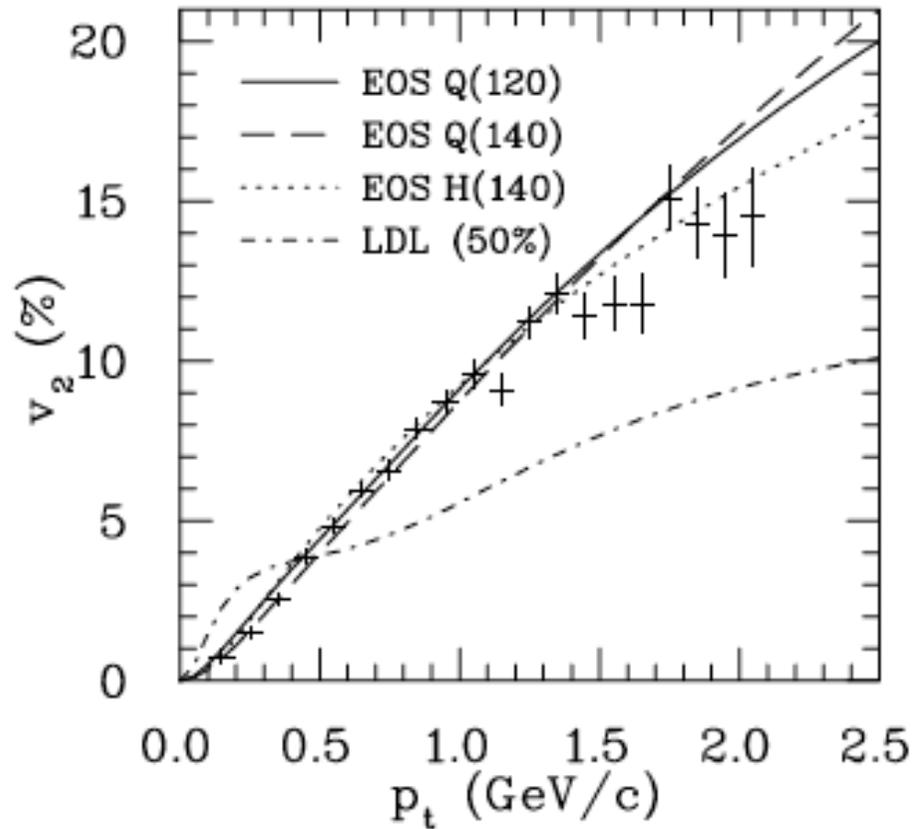
- ❖ Both scenarios explain 0-10% Au+Au 200 GeV data on charged hadron  $p_T$  spectra.
- ❖ However  $x = 1$  explains better elliptic flow ( $v_2$ ) in 0-10% centrality.
- ❖ Geometric scaling of Au+Au collisions changes with collision centrality
- ❖ Central collision  $\sim$  energy density scales with binary collision (hard processes)
- ❖ Less central  $\sim$  number of participant (soft processes)

THANK YOU  
THANK YOU

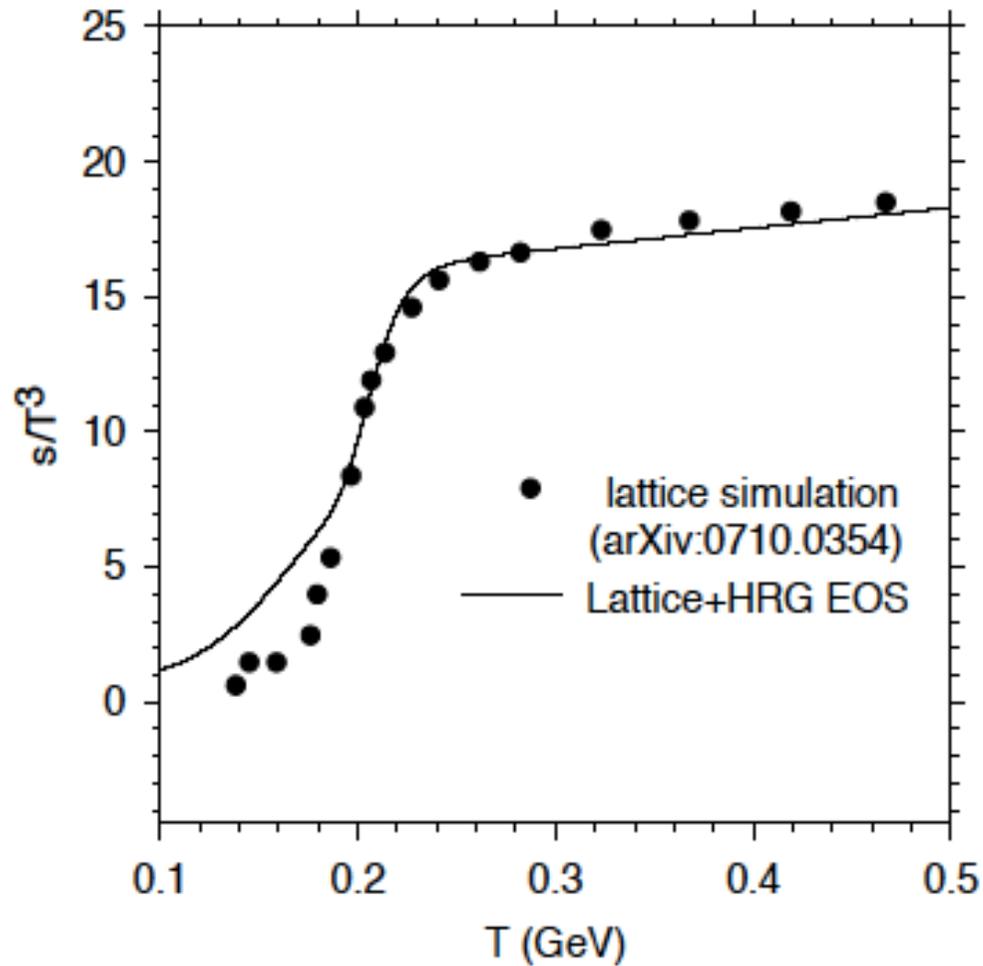
Thanks to the Organizers for local support  
And  
Department of Science and Technology ,Govt. of India for travel support.

# Back up

Charged Hadron AuAu 130 STAR, heinz



## Combined EOS



$$\frac{s}{T^3} = \alpha + [\beta + \gamma T] \left[ 1 + \tanh \frac{T - T_c}{\Delta T} \right],$$

$$p(T) = \int_0^T s(T') dT'$$

$$\varepsilon(T) = Ts - p.$$